

	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12		
	Algebraic Thinking							Place Value and Proportion						
Autumn	Sequences		Understand and use algebraic notation		Equality and equivalence		Place value and ordering integers and decimals		Fraction, decimal and percentage equivalence					
	Applications of Number						Directed Number			Fractional Thinking				
Spring	with addition wit		with i	Solving problems vith multiplication serventages of and division		Fractions & percentages of amounts	Operations and equations with directed number		Addition and subtraction of fractions					
	Lines and Angles						Reasoning with Number							
Summer	Constructing, measuring and using geometric notation			Developing geometric reasoning			Devel num ser	nber	Sets and probability		Prii numbe pro			



## Sequences

- Describe and continue a sequence given diagrammatically
- Predict and check the next term(s) of a sequence
- Represent sequences in tabular and graphical forms
- Recognise the difference between linear and non-linear sequences
- Continue numerical linear sequences
- Continue numerical non-linear sequences
- Explain the term-to-term rule of numerical sequences in words
- Find missing numbers within sequences



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### Understand and use notation

- Given a numerical input, find the output of a single function machine
- Use inverse operations to find the input given the output
- Use diagrams and letters to generalise number operations
- Use diagrams and letters with single function machines
- Find the function machine given a simple expression
- Substitute values into single operation expressions
- Find numerical inputs and outputs for a series of two function machines
- Use diagrams and letters with a series of two function machines
- Find the function machines given a two-step expression
- Substitute values into two-step expressions
- Generate sequences given an algebraic rule
- Represent one- and two-step functions graphically



# **Equality and Equivalence**

- Understand the meaning of equality
- Understand and use fact families, numerically and algebraically
- $\blacksquare$  Solve one-step linear equations involving +/- using inverse operations
- Solve one-step linear equations involving  $\times/\div$  using inverse operations
- Understand the meaning of like and unlike terms
- Understand the meaning of equivalence
- $\blacksquare$  Simplify algebraic expressions by collecting like terms, using the  $\equiv$  symbol



### Place Value

- Recognise the place value of any number in an integer up to one billion
- Understand and write integers up to one billion in words and figures
- Work out intervals on a number line
- Position integers on a number line
- Round integers to the nearest power of ten
- Compare two numbers using =,  $\neq$ , <, >,  $\leq$ ,  $\geq$
- Order a list of integers
- Find the range of a set of numbers
- Find the median of a set of numbers
- Understand place value for decimals
- Position decimals on a number line
- Compare and order any number up to one billion



### Place Value

#### Small Steps

Round a number to 1 significant figure	
Write 10, 100, 1000 etc. as powers of ten	H
Write positive integers in the form A x 10 <sup>n</sup>	H
Investigate negative powers of ten	H
Write decimals in the form A x 10 <sup>n</sup>	H



## FDP Equivalence

#### Small Steps

- Represent tenths and hundredths as diagrams
- Represent tenths and hundredths on number lines
- Interchange between fractional and decimal number lines
- Convert between fractions and decimals tenths and hundredths
- Convert between fractions and decimals fifths and quarters
- Convert between fractions and decimals eighths and thousandths



- Understand the meaning of percentage using a hundred square
- Convert fluently between simple fractions, decimals and percentages
- Use and interpret pie charts
  - H



## FDP Equivalence

#### Small Steps

- Represent any fraction as a diagram
- Represent fractions on number lines
- Identify and use simple equivalent fractions
- Understand fractions as division
- Convert fluently between fractions, decimals and percentages
- Explore fractions above one, decimals and percentages





### Addition and Subtraction

- Properties of addition and subtraction
- Mental strategies for addition and subtraction
- Use formal methods for addition of integers
- Use formal methods for addition of decimals
- Use formal methods for subtraction of integers
- Use formal methods for subtraction of decimals
- Choose the most appropriate method: mental strategies, formal written or calculator
- Solve problems in the context of perimeter
- Solve financial maths problems



### Addition and Subtraction

#### Small Steps

- Solve problems involving tables and timetables
- Solve problems with frequency trees
- Solve problems with bar charts and line charts
- Add and subtract numbers given in standard form



H



## Multiplication and Division

#### Small Steps

- Properties of multiplication and division
- Understand and use factors
- Understand and use multiples
- Multiply and divide integers and decimals by powers of 10
- Multiply by 0.1 and 0.01

H

- Convert metric units
- Use formal methods to multiply integers
- Use formal methods to multiply decimals
- Use formal methods to divide integers
- Use formal methods to divide decimals



## Multiplication and Division

#### Small Steps

- Understand and use order of operations
- Solve problems using the area of rectangles and parallelograms
- Solve problems using the area of triangles
- Solve problems using the area of trapezia

H

- Solve problems using the mean
- Explore multiplication and division in algebraic expressions





## Fractions & Percentages of Amounts

#### Small Steps

- Find a fraction of a given amount
- Use a given fraction to find the whole and/or other fractions
- Find a percentage of a given amount using mental methods
- Find a percentage of a given amount using a calculator
- Solve problems with fractions greater than 1 and percentages greater than 100%



H



### **Directed Number**

- Understand and use representations of directed numbers
- Order directed numbers using lines and appropriate symbols
- Perform calculations that cross zero
- Add directed numbers
- Subtract directed numbers
- Multiplication of directed numbers
- Multiplication and division of directed numbers
- Use a calculator for directed number calculations
- Evaluate algebraic expressions with directed number
- Introduction to two-step equations



#### **Directed Number**

#### Small Steps

- Solve two-step equations
- Use order of operations with directed numbers
- Roots of positive numbers
- Explore higher powers and roots

H





# Fractional Thinking

- Understand representations of fractions
- Convert between mixed numbers and fractions
- Add and subtract unit fractions with the same denominator
- Add and subtract fractions with the same denominator
- Add and subtract fractions from integers expressing the answer as a single fraction
- Understand and use equivalent fractions
- Add and subtract fractions where denominators share a simple common multiple
- Add and subtract fractions with any denominator
- Add and subtract improper fractions and mixed numbers
- Use fractions in algebraic contexts
- Use equivalence to add and subtract decimals and fractions
- Add and subtract simple algebraic fractions





# Fractional Thinking

#### **Small Steps**

- Use fractions in algebraic contexts
- Use equivalence to add and subtract decimals and fractions
- Add and subtract simple algebraic fractions





## Construction and Measuring

- Understand and use letter and labelling conventions including those for geometric figures
- Draw and measure line segments including geometric figures
- Understand angles as a measure of turn
- Classify angles
- Measure angles up to 180°
- Draw angles up to 180°
- Draw and measure angles between 180° and 360°
- Identify perpendicular and parallel lines
- Recognise types of triangle
- Recognise types of quadrilateral



## Construction and Measuring

- Identify polygons up to a decagon
- Construct triangles using SSS
- Construct triangles using SSS, SAS and ASA
- Construct more complex polygons
- Interpret simple pie charts using proportion
- Interpret pie charts using a protractor
- Draw pie charts



## Geometric Reasoning

- Understand and use the sum of angles at a point
- Understand and use the sum of angles on a straight line
- Understand and use the equality of vertically opposite angles
- Know and apply the sum of angles in a triangle
- Know and apply the sum of angles in a quadrilateral
- Solve angle problems using properties of triangles and quadrilaterals
- Solve complex angle problems



# Geometric Reasoning

### **Small Steps**

Find and use the angle sum of any polygon	H
Investigate angles in parallel lines	H
Understand and use parallel line angle rules	H
Use known facts to obtain simple proofs.	H



## **Developing Number Sense**

- Know and use mental addition and subtraction strategies for integers
- Know and use mental multiplication and division strategies for integers
- Know and use mental arithmetic strategies for decimals
- Know and use mental arithmetic strategies for fractions
- Use factors to simplify calculations
- Use estimation as a method for checking mental calculations
- Use known number facts to derive other facts
- Use known algebraic facts to derive other facts
- Know when to use a mental strategy, formal written method or a calculator



# Sets and Probability

#### Small Steps

- Identify and represent sets
- Interpret and create Venn diagrams
- Understand and use the intersection of sets
- Understand and use the union of sets
- Understand and use the complement of a set
- Know and use the vocabulary of probability





# Sets and Probability

#### Small Steps

- Generate sample spaces for single events
- Calculate the probability of a single event
- Understand and use the probability scale
- Know that the sum of probabilities of all possible outcomes is 1



## Prime Numbers and Proof

- Find and use multiples
- Identify factors of numbers and expressions
- Recognise and identify prime numbers
- Recognise square and triangular numbers
- Find common factors of a set of numbers including the HCF
- Find common multiples of a set of numbers including the LCM
- Write a number as a product of its prime factors
- Use a Venn diagram to calculate the HCF and LCM



- Make and test conjectures
- Use counterexamples to disprove a conjecture
  - H denotes higher strand and not necessarily content for Higher Tier GCSE



	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12	
	Proportional Reasoning						Representations						
Autumn		and ale	Multiplicative change		Multiplying and dividing fractions		Working in the Cartesian plane		Representing data		Tables & Probability		
	Algebraic techniques						Developing Number						
Spring	Brackets, equations and inequalities					Indices		Fractions and percentages		index i		lumber sense	
	Developing Geometry					Reasoning with Data							
Summer	Angles in parallel lines and polygons			circles   So P		Line symmetry and reflection	The data handling cycle		ycle	Measures of location			



### Ratio and Scale

- Understand the meaning and representation of ratio
- Understand and use ratio notation
- $\blacksquare$  Solve problems involving ratios of the form 1: n (or n: 1)
- Solve proportional problems involving the ratio m:n
- Divide a value into a given ratio
- Express ratios in their simplest integer form
- $\blacksquare$  Express ratios in the form 1: n
- Compare ratios and related fractions
- $\blacksquare$  Understand  $\pi$  as the ratio between diameter and circumference
- Understand gradient of a line as a ratio
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# **Multiplicative Change**

### Small Steps

- Solve problems involving direct proportion
- Explore conversion graphs
- Convert between currencies
- Explore direct proportion graphs

- Explore relationships between similar shapes
- Understand scale factors as multiplicative representations
- Draw and interpret scale diagrams
- Interpret maps using scale factors and ratios



# **Multiplying & Dividing Fractions**

- Represent multiplication of fractions
- Multiply a fraction by an integer
- Find the product of a pair of unit fractions
- Find the product of a pair of any fractions
- Divide an integer by a fraction
- Divide a fraction by a unit fraction
- Understand and use the reciprocal
- Divide any pair of fractions



# **Multiplying & Dividing Fractions**

#### Small Steps

Multiply and divide improper and mixed fractions

H

Multiply and divide algebraic fractions

H

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R

denotes "review step" – content should have been covered earlier in KS3



# Working in the Cartesian Plane

#### Small Steps

- Work with coordinates in all four quadrants
- Identify and draw lines that are parallel to the axes
- Recognise and use the line y = x
- Recognise and use lines of the form y = kx
- Link y = kx to direct proportion problems
- Explore the gradient of the line y=kx

H

- Recognise and use lines of the form y = x + a
- Explore graphs with negative gradient (y = -kx, y = a x, x + y = a)
  - H



# Working in the Cartesian Plane

- Link graphs to linear sequences
- Plot graphs of the form y = mx + c
- Explore non-linear graphs
- Find the midpoint of a line segment







## Representing Data

- Draw and interpret scatter graphs
- Understand and describe linear correlation
- Draw and use line of best fit
- Identify non-linear relationships
- Identify different types of data
- Read and interpret ungrouped frequency tables
- Read and interpret grouped frequency tables
- Represent grouped discrete data
- Represent continuous data grouped into equal classes
- Represent data in two-way tables



# Tables and Probability

#### Small Steps

- Construct sample spaces for 1 or more events
- Find probabilities from a sample space
- Find probabilities from two-way tables
- Find probabilities from Venn diagrams
- Use the product rule for finding the total number of possible outcomes







# Brackets, Equations & Inequalities

#### Small Steps

- Form algebraic expressions
- Use directed number with algebra
- Multiply out a single bracket
- Factorise into a single bracket
- Expand multiple single brackets and simplify
- Expand a pair of binomials
- Solve equations, including with brackets
- Form and solve equations with brackets
- Understand and solve simple inequalities
  - H



# Brackets, Equations & Inequalities

#### Small Steps

- Form and solve inequalities
- Solve equations and inequalities with unknowns on both sides

H

Form and solve equations and inequalities with unknowns on both sides

H

Identify and use formulae, expressions, identities and equations





## Sequences

### Small Steps

- Generate sequences given a rule in words
- Generate sequences given a simple algebraic rule
- Generate sequences given a complex algebraic rule
- Find the rule for the  $oldsymbol{n}^{\mathsf{th}}$  term of a linear sequence



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### **Indices**

### Small Steps

- Adding and subtracting expressions with indices
- Simplifying algebraic expressions by multiplying indices
- Simplifying algebraic expressions by dividing indices
- Using the addition law for indices
- Using the addition and subtraction law for indices
- Exploring powers of powers



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# Fractions and Percentages

### Small Steps

Convert fluently between key fractions, decimals and percentages

W

Calculate key fractions, decimals and percentages of an amount without a calculator

- R
- Calculate fractions, decimals and percentages of an amount using calculator methods
- R

- Convert between decimals and percentages greater than 100%
- Percentage decrease with a multiplier
- Calculate percentage increase and decrease using a multiplier
- Express one number as a fraction or a percentage of another without a calculator
- Express one number as a fraction or a percentage of another using calculator methods
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## Fractions and Percentages

- Work with percentage change
- Choose appropriate methods to solve percentage problems
- Find the original amount given the percentage less than 100%
- Find the original amount given the percentage greater than 100%
- Choose appropriate methods to solve complex percentage problems

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### Standard Form

- Investigate positive powers of 10
- Work with numbers greater than 1 in standard form
- Investigate negative powers of 10
- Work with numbers between 0 and 1 in standard form
- Compare and order numbers in standard form
- Mentally calculate with numbers in standard form
- Add and subtract numbers in standard form
- Multiply and divide numbers in standard form
- Use a calculator to work with numbers in standard form
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### Standard Form

#### Small Steps

Understand and use negative indices

H

Understand and use fractional indices

H

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### **Number Sense**

- Round numbers to powers of 10, and 1 significant figure
- Round numbers to a given number of decimal places
- Estimate the answer to a calculation
- Understand and use error interval notation
- Calculate using the order of operations
- Calculate with money
- Covert metric measures of length
- Convert metric units of weight and capacity
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### **Number Sense**

### Small Steps

Convert metric units of area

H

Convert metric units of volume

H

Solve problems involving time and the calendar

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# Angles in parallel lines & polygons

- Understand and use basic angles rules and notation
- Investigate angles between parallel lines and the transversal
- Identify and calculate with alternate and corresponding angles
- Identify and calculate with co-interior, alternate and corresponding angles
- Solve complex problems with parallel line angles
- Construct triangles and special quadrilaterals
- Investigate the properties of special quadrilaterals
- Identify and calculate with sides and angles in special quadrilaterals
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# Angles in parallel lines & polygons

### Small Steps

Understand and use the properties of diagonals of quadrilaterals

Understand and use the sum of exterior angles of any polygon

Calculate and use the sum of the interior angles in any polygon

Calculate missing interior angles in regular polygons

Prove simple geometric facts

Construct an angle bisector

Construct a perpendicular bisector of a line segment

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# Area of Trapezia and Circles

### Small Steps

- Calculate the area of triangles, rectangles and parallelograms
- and the area of the second second per attentions
- Calculate the perimeter and area of compound shapes (1)
- Investigate the area of a circle

Calculate the area of a trapezium

- Calculate the area of a circle and parts of a circle without a calculator
- Calculate the area of a circle and parts of a circle with a calculator
- Calculate the perimeter and area of compound shapes (2)

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## Line symmetry and reflection

- Recognise line symmetry
- Reflect a shape in a horizontal or vertical line 1 (shapes touching the line)
- Reflect a shape in a horizontal or vertical line 2 (shapes not touching the line)
- Reflect a shape in a diagonal line 1 (shapes touching the line)
- Reflect a shape in a diagonal line 2 (shapes not touching the line)

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# The Data Handling Cycle

- Set up a statistical enquiry
- Design and criticise questionnaires
- Draw and interpret pictograms, bar charts and vertical line charts
- Draw and interpret multiple bar charts
- Draw and interpret pie charts
- Draw and interpret line graphs
- Choose the most appropriate diagram for given set of data
- Represent and interpret grouped quantitative data
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# The Data Handling Cycle

- Find and interpret the range
- Compare distributions using charts
- Identify misleading graphs

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### Measures of Location

- Understand and use the mean, median and mode
- Choose the most appropriate average
- Find the mean from an ungrouped frequency table
- Find the mean from an grouped frequency table
- Identify outliers
- Compare distributions using averages and the range

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	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12
	Reasoning with Algebra						Constructing in 2 and 3 Dimensions					
Autumn	Straight line graphs		Forming and solving equations		Testing conjectures		Three-dimensional shapes		Constructions and congruency			
Spring	Reasoning with Number						Reasoning with Geometry					
	Numbers		Using percentages		Maths and money		Deduction :		on and Pythagoras' lation Theorem		_	
Summer	Reasoning with Proportion						Representations and Revision					
	Enlargement and similarity		Solving ratio & proportion R problems		Ra	tes	Probability		Algebraic representation		Revision	



# Straight line graphs

#### Small Steps

Lines parallel to the axes, y = x and y = -x

Using tables of values

R

- Compare gradients
- Compare intercepts
- Understand and use y = mx + c
- Write an equation in the form y = mx + c



- Find the equation of a line from a graph
- Interpret gradient and intercepts of real-life graphs
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## Straight line graphs

### **Small Steps**

Model real-life graphs involving inverse proportion

H

Explore perpendicular lines

H

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### Forming and solving equations

- Solve one- and two-step equations and inequalities
- Solve one- and two-step equations and inequalities with brackets
- Inequalities with negative numbers
- Solve equations with unknowns on both sides
- Solve inequalities with unknowns on both sides
- Solving equations and inequalities in context
- Substituting into formulae and equations
- Rearrange formulae (one-step)
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### Forming and Solving Equations

- Rearrange formulae (two-step)
- Rearrange complex formulae including brackets and squares

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### Testing conjectures

- Factors, Multiples and Primes
- True or False?
- Always, Sometimes, Never true
- Show that
- Conjectures about number
- Expand a pair of binomials
- Conjectures with algebra
- Explore the 100 grid
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### Testing conjectures

### **Small Steps**

Expand three binomials



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# Three-dimensional shapes

- Know names of 2-D and 3-D shapes
- Recognise prisms
- Accurate nets of cuboids and other 3-D shapes
- Sketch and recognise nets of cuboids and other 3-D shapes
- Plans and elevations
- Find area of 2-D shapes
- Surface area of cubes and cuboids
- Surface area of triangular prisms
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# Three-dimensional shapes

### Small Steps

- Surface area of a cylinder
- Volume of cubes and cuboids
- Volume of other 3-D shapes prisms and cylinders
- Explore volumes of cones, pyramids and spheres

H

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# Constructions & congruency

- Draw and measure angles
- Construct and interpret scale drawings
- Locus of distance from a point
- Locus of distance from a straight line/shape
- Locus equidistant from two points
- Construct a perpendicular bisector
- Construct a perpendicular from a point
- Construct a perpendicular to a point
  - H denotes higher strand and not necessarily content for Higher Tier GCSE
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# Constructions & congruency

- Locus of distance from two lines
- Construct an angle bisector
- Construct triangles from given information
- Identify congruent figures
- Explore congruent triangles
- Identify congruent triangles

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### **Numbers**

- Integers, real and rational numbers
- Understand and use surds
- Work with directed number
- Solve problems with integers
- Solve problems with decimals
- HCF and LCM
- Adding and subtracting fractions
- Multiplying and dividing fractions
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### **Numbers**

- Solving problems with fractions
- Numbers in standard form

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### Using percentages

Use the equivalence of fractions, decimals and percentages	R
Calculate percentage increase and decrease	R
Express a change as a percentage	R
Solve 'reverse' percentage problems	
Recognise and solve percentage problems (non-calculator)	
Recognise and solve percentage problems (calculator)	R
Solve problems with repeated percentage change	H

- H denotes higher strand and not necessarily content for Higher Tier GCSE
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### Maths and Money

- Solve problems with bills and bank statements
- Calculate simple interest
- Calculate compound interest
- Solve problems with Value Added Tax
- Calculate wages and taxes
- Solve problems with exchange rates
- Solve unit pricing problems

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### **Deduction**

- Angles in parallel lines
- Solving angles problems (using chains of reasoning)
- Angles problems with algebra
- Conjectures with angles
- Conjectures with shapes
- Link constructions and geometrical reasoning

- Holdenotes higher strand and not necessarily content for Higher Tier GCSE
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### Rotation and Translation

- Identify the order of rotational symmetry of a shape
- Compare and contrast rotational symmetry with line symmetry
- Rotate a shape about a point on a shape
- Rotate a shape about a point not on a shape
- Translate points and shapes by a given vector
- Compare rotation and reflection of shapes
- Find the result of a series of transformations



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# Pythagoras' Theorem

- Squares and square roots
- Identify the hypotenuse of a right-angled triangle
- Determine whether a triangle is right-angled
- Calculate the hypotenuse of a right-angled triangle
- Calculate missing sides in right-angled triangles
- Use Pythagoras theorem on coordinate axes
- Explore proofs of Pythagoras' theorem
- Use Pythagoras' theorem in 3-D shapes
  - denotes higher strand and not necessarily content for Higher Tier GCSE
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# **Enlargement and Similarity**

- Recognise enlargement and similarity
- Enlarge a shape by a positive integer scale factor
- Enlarge a shape by a positive integer scale factor from a point
- Enlarge a shape by a positive fractional scale factor
- Enlarge a shape by a negative scale factor
- Work out missing sides and angles in a pair of given similar shapes
- Solve problems with similar triangles
- Explore ratios in right-angled triangles
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# Ratio and Proportion

Solve problems with direct proportion	R
Direct proportion and conversion graphs	R
Solve problems with inverse proportion	
Graphs of inverse relationships	H
Solve ratio problems given the whole or a part	R
Solve 'best buy' problems	
Solve problems ratio and algebra	H

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### Rates

- Solve speed, distance and time problems without a calculator
- Solve speed, distance and time problems with a calculator
- Use distance/time graphs
- Solve problems with density, mass and volume
- Solve flow problems and their graphs
- Rates of change and their units
- Convert compound units



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# **Probability**

## Small Steps

Single event probability
 Relative frequency – include convergence
 Expected outcomes
 Independent events
 Use tree diagrams
 Use tree diagrams to solve 'without replacement' problems
 Use diagrams to work out probabilities

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# Algebraic representation

- Draw and interpret quadratic graphs
- Interpret graphs, including reciprocal and piece-wise
- Investigate graphs of simultaneous equations
- Represent inequalities

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### Revision

#### **Suggestions**

The content for the last three weeks of Year 9 is not specified.

You can use their assessment of students' progress over Key Stage to identify any key areas that need to be addressed and focus on these before embarking on KS4.

Below are some suggestions of topic areas that might be useful to revise as some of the content has not been covered for some time, but this list is neither intended as prescriptive nor exhaustive.

Representing Number	Representing Data	Algebraic Representations	Representing Problems			
<ul><li>Standard form</li><li>Product of primes</li><li>Error intervals</li></ul>	<ul><li>Scatter graphs</li><li>Statistical graphs</li><li>Measures</li><li>Tables and timetables</li><li>Data handling project</li></ul>	<ul> <li>Find the rule for the n<sup>th</sup> term of a sequence</li> <li>Investigating algebraic proof</li> </ul>	Using graphs, equations, tables etc. to solve complex word problems			



	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12		
	Similarity							Developing Algebra						
Autumn	Congruence, similarity and Trigen				gonometry		Representing solutions of equations and inequalities			Simultaneous equations				
	Geometry						Proportions and Proportional Change							
Spring	Angles & Working with bearings circles				Vec	tors	ļ.	Ratios & Percentages fractions and Interest		Probability				
	Delving into data						Using number Expressions							
Summer	Collecting, representing and interpreting data				calcu	on- ulator hods	numb	es of er and ences	! ]	es and ots	and Manipulatin			



# Congruence, Similarity and Enlargement

- Enlarge a shape by a positive integer scale factor
- Enlarge a shape by a fractional scale factor
- Enlarge a shape by a negative scale factor
- Identify similar shapes
- Work out missing sides and angles in a pair given similar shapes
- Use parallel line rules to work out missing angles
- Establish a pair of triangles are similar

- denotes Higher Tier GCSE content
- R denotes 'review step' content should have been covered at KS3



# Congruence, Similarity and Enlargement

- Explore areas of similar shapes
- Explore volumes of similar shapes
- Solve mixed problems involving similar shapes
- Understand the difference between congruence and similarity
- Understand and use conditions for congruent triangles
- Prove a pair of triangles are congruent

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# Trigonometry

- Explore ratio in similar right-angled triangles
- Work fluently with the hypotenuse, opposite and adjacent sides
- Use the tangent ratio to find missing side lengths
- Use the sine and cosine ratio to find missing side lengths
- Use sine, cosine and tangent to find missing side lengths
- Use sine, cosine and tangent to find missing angles
- Calculate sides in right-angled triangles using Pythagoras' Theorem
- Select the appropriate method to solve right-angled triangle problems
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# Trigonometry

- Work with key angles in right-angled triangles
- Use trigonometry in 3-D shapes
- Use the formula  $\frac{1}{2}ab\sin C$  to find the area of a triangle
- Understand and use the sine rule to find missing lengths
- Understand and use the sine rule to find missing angles
- Understand and use the cosine rule to find missing lengths
- Understand and use the cosine rule to find missing angles
- Choosing and using the sine and cosine rules
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# **Equations and Inequalities**

- Understand the meaning of a solution
- Form and solve one-step and two-step equations
- Form and solve one-step and two-step inequalities
  - Show solutions to inequalities on a number line
  - Interpret representations on number lines as inequalities
  - Represent solutions to inequalities using set notation
- Draw straight line graphs
- Find solutions to equations using straight line graphs
  - H denotes Higher Tier GCSE content
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## **Equations and Inequalities**

- Represent solutions to single inequalities on a graph
- Represent solutions to multiple inequalities on a graph
- Form and solve equations with unknowns on both sides
- Form and solve inequalities with unknowns on both sides
- Form and solve more complex equations and inequalities
- Solve quadratic equations by factorisation\* (\*Also Foundation tier. Higher cover now, Core will cover in Year 11)
- Solve quadratic inequalities in one variable

- H denotes Higher Tier GCSE content
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## Simultaneous Equations

- Understand that equations can have more than one solution
- Determine whether a given (x, y) is a solution to a pair of linear simultaneous equations
- Solve a pair of linear simultaneous equations by substituting a known variable
- Solve a pair of linear simultaneous equations by substituting an expression
- Solve a pair of linear simultaneous equations using graphs
- Solve a pair of linear simultaneous equations by subtracting equations
- Solve a pair of linear simultaneous equations by adding equations
- Use a given equation to derive related facts
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## Simultaneous Equations

- Solve a pair of linear simultaneous equations by adjusting one equation
- Solve a pair of linear simultaneous equations by adjusting both equations
- Form a pair of linear simultaneous equations from given information
- Form and solve pair of linear simultaneous equations from given information
- $\blacksquare$  Determine whether a given (x, y) is a solution to both a linear and quadratic equation
- Solve a pair of simultaneous equations (one linear, one quadratic) using graphs
- Solve a pair of simultaneous equations (one linear, one quadratic) algebraically
- Solve a pair of simultaneous equations involving a third unknown
  - denotes Higher Tier GCSE content
  - R denotes 'review step' content should have been covered at KS3



# **Angles and Bearings**

- Use cardinal directions and related angles
- Draw and interpret scale diagrams
- Understand and represent bearings
- Measure and read bearings
- Make scale drawings using bearings
- Calculate bearings using angles rules
- Solve bearings problems using Pythagoras and trigonometry
- Solve bearings problems using the sine and cosine rules
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  - R denotes 'review step' content should have been covered at KS3



## Working with Circles

- Recognise and label parts of a circle
- Calculate fractional parts of a circle
- Calculate the length of an arc
- Calculate the area of a sector
- Circle theorem: Angles at the centre and circumference
- Circle theorem: Angles in a semicircle
  - Circle theorem: Angles in the same segment
  - Circle theorem: Angles in a cyclic quadrilateral
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## Working with Circles

- Understand and use the volume of a cylinder and cone
- Understand and use the volume of a sphere
- Understand and use the surface area of a sphere
- Understand and use the surface area of a cylinder and cone
- Solve area and volume problems involving similar shapes





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### **Vectors**

- Understand and represent vectors
- Use and read vector notation
- Draw and understand vectors multiplied by a scalar
- Draw and understand addition of vectors
- Draw and understand addition and subtraction of vectors
- Explore vector journeys in shapes
- Explore quadrilaterals using vectors
- Understand parallel vectors
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### **Vectors**

- **Explore collinear points using vectors**
- Use vectors to construct geometric arguments and proofs

- H

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## **Ratios and Fractions**

- Compare quantities using a ratio
- Link ratios and fractions
- Share in a ratio (given total or one part)
- Use ratios and fractions to make comparisons
- Link ratios and graphs
- Solve problems with currency conversion
- Link ratios and scales
- Use and interpret ratios of the form 1:n and n:1
- Solve 'best buy' problems
- Combine a set of ratios
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## Ratios and Fractions

- Link ratio and algebra
- Ratio in area problems
- Ratio in volume problems
- Mixed ratio problems

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## Percentages & Interest

- Convert and compare fractions, decimals and percentages
- Work out percentages of amounts (with and without a calculator)
- Increase and decrease by a given percentage
- Express one number as a percentage of another
- Calculate simple and compound interest
- Repeated percentage change
- Find the original value after a percentage change
- Solve problems involving growth and decay
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## Percentages & Interest

### Small Steps

Understand iterative processes



Solve problems involving percentages, ratios and fractions

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# **Probability**

- Know how to add, subtract and multiply fractions
- Find probabilities using equally likely outcomes
- Use the property that probabilities sum to 1
- Using experimental data to estimate probabilities
- Find probabilities from tables, Venn diagrams and frequency trees
- Construct and interpret sample spaces for more than one event
- Calculate probability with independent events
- Use tree diagrams for independent events
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  - R denotes 'review step' content should have been covered at KS3



# **Probability**

- Use tree diagrams for dependent events
- Construct and interpret conditional probabilities (Tree diagrams)

- Construct and interpret conditional probabilities (Venn diagrams and two-way tables)
- H

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- R denotes 'review step' content should have been covered at KS3



## Delving into data

#### Small Steps

- Understand populations and samples
- Construct a stratified sample

H

- Primary and secondary data
- Construct and interpret frequency tables and frequency polygons
- Construct and interpret two-way tables

R

- Construct and interpret line and bar charts (including composite bar charts)
- Construct and interpret pie charts

R

- Criticise charts and graphs
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# Delving into data

### Small Steps

Construct histograms	H
Interpret histograms	H
Find and interpret averages from a list	R
Find and interpret averages from a table	R
Construct and interpret time series graphs	R
Construct and interpret stem-and-leaf diagrams	
Construct and interpret cumulative frequency diagrams	H
Use cumulative frequency diagrams to find measures	H

denotes 'review step' – content should have been covered at KS3

denotes Higher Tier GCSE content



## Delving into data

Understand extrapolation

### Small Steps

Compare distributions using charts and measures

Compare distributions using complex charts and measures

Construct and interpret scatter graphs

Draw and use a line of best fit

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## Non-calculator methods

Mental/written methods of integer/decimal addition and subtraction	R
Mental/written methods of integer/decimal multiplication and division	R
The four rules of fraction arithmetic	R
Exact answers	
Rational and irrational numbers (convert recurring decimals here)	H
Understand and use surds	H
Calculate with surds	H
Rounding to decimal places and significant figures	R

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- R denotes 'review step' content should have been covered at KS3



## Non-calculator methods

- Estimating answers to calculations
- Understand and use limits of accuracy
- Upper and lower bounds
- Use number sense
- Solve financial maths problems
- Break down and solve multi-step problems

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- R denotes 'review step' content should have been covered at KS3



### Types of Number and Sequences

#### Small Steps

Understand the difference between factors and multiples

Understand primes and express a number as a product of its prime factors

Find the HCF and LCM of a set of numbers

Describe and continue arithmetic and geometric sequences

Explore other sequences

Describe and continue sequences involving surds

Find the rule for the nth term of a linear sequence

H denotes Higher Tier GCSE content

Find the rule for the  $n^{\text{th}}$  term of a quadratic sequence

R denotes 'review step' – content should have been covered at KS3



## Indices and Roots

- Square and Cube numbers
   Calculate higher powers and roots
   Powers of ten and standard form
   The addition and subtraction rules for indices
   Understand and use the power zero and negative indices
   Work with powers of powers
   Understand and use fractional indices
   Calculate with numbers in standard form
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  - R denotes 'review step' content should have been covered at KS3



## Manipulating expressions

Simplify algebraic expressions	R
Use identities	
Add and subtract simple algebraic fractions	H
Add and subtract complex algebraic fractions	H
Multiply and divide simple algebraic fractions	H
Multiply and divide complex algebraic fractions	H
Form and solve equations and inequalities with fractions	
Solve equations with algebraic fractions	H

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## Manipulating expressions

- Represent numbers algebraically
- Algebraic arguments and proof

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	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12		
	Graphs							Algebra						
Autumn	Gradients & lines		Non-linear graphs		Using graphs		Expanding & factorising		Changing the subject		Functions			
	Reasoning						Revision and Communication							
Spring	Multiplicative Geometric		netric	Algebraic		Transforming& constructing		describing & Show that		that				
Summer	Revision								Examiı	nations				



## **Gradients & lines**

#### Small Steps

Equations of lines parallel to the axis

Plot straight line graphs

Interpret y = mx + c

Find the equation of a straight line from a graph (1)

Find the equation of a straight line from a graph (2)

Equation of a straight-line graph given one point and gradient

Equation of a straight-line graph given two points

Determine whether a point is on a line

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## Gradients & lines

#### Small Steps

Solve linear simultaneous equations graphically

R

Recognise when straight lines are perpendicular

H

Find the equations of perpendicular lines

H

- denotes Higher Tier GCSE content
- R denotes 'review step' content should have been covered at KS3



## Non-linear graphs

- Plot and read from quadratic graphs
- Plot and read from cubic graphs
- Plot and read from reciprocal graphs
- Recognise graph shapes
- Identify and interpret roots and intercepts of quadratics
- Understand and use exponential graphs
- Find and use the equation of a circle centre (0, 0)
- Find the equation of the tangent to any curve
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# Using graphs

## Small Steps

Reflect shapes in given lines

Construct and interpret conversion graphs

R

Construct and interpret other real-life straight line graphs

R

- Interpret distance/time graphs
- Construct distance/time graphs
- Construct and interpret speed/time graphs
- Construct and interpret piece-wise graphs
- Recognise and interpret graphs that illustrate direct and inverse proportion
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# Using graphs

## Small Steps

- Find approximate solutions to equations using graphs
- Estimate the area under a curve

W

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- R denotes 'review step' content should have been covered at KS3



# **Expanding and factorising**

#### Small Steps

Expand and factorise with a single bracket Expand binomials Factorise quadratic expressions Factorise complex quadratic expressions Solve equations equal to 0 Solve quadratic equations by factorisation Solve complex quadratic expressions by factorisation Complete the square

denotes 'review step' - content should have been covered at KS3

denotes Higher Tier GCSE content



# Expanding and factorising

### **Small Steps**

Solve quadratic equations using the quadratic formula



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# Changing the subject

### Small Steps

Solve linear equations Solve inequalities Form and solve equations and inequalities in the context of shape Change the subject of a simple formula Change the subject of a known formula Change the subject of a complex formula Change the subject where the subject appears more than once Solve equations by iteration

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### **Functions**

#### Small Steps

Use function machines
 Substitute into expressions and formulae
 Use function notation
 Work with composite functions
 Work with inverse functions
 Graphs of quadratic functions
 Solve quadratic inequalities

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Understand and use trigonometric functions

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# Multiplicative Reasoning

### **Small Steps**

Use scale factors
 Understand direct proportion
 Construct complex direct proportion equations
 Calculate with pressure and density
 Understand inverse proportion
 Construct inverse proportion equations
 Ratio problems

- H denotes Higher Tier GCSE content
- R denotes 'review step' content should have been covered at KS3



## Geometric Reasoning

#### Small Steps

Angles at points Angles in parallel lines and shapes Exterior and interior angles of polygons Proving geometric facts Solve problems involving vectors The first four circle theorems Angle between a radius and a chord Angle between a radius and a tangent

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denotes Higher Tier GCSE content



## Geometric Reasoning

### Small Steps

Two tangents from a point
 Alternate segment theorem
 Pythagoras' theorem and trigonometrical ratios

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- R denotes 'review step' content should have been covered at KS3



# Algebraic Reasoning

### **Small Steps**

Simplify complex expressions
 Find the rule for the n<sup>th</sup> term of a linear sequence
 Find the rule for the n<sup>th</sup> term of a quadratic sequence
 Use rules for sequences
 Solve linear simultaneous equations
 Solve simultaneous equations with one quadratic
 Formal algebraic proof
 Inequalities in two variables

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## Transforming and Constructing

Perform and describe line symmetry and reflection	R
Perform and describe rotation/rotational symmetry	R
Perform and describe translations of shapes	R
Perform and describe enlargements of shapes	R
Perform and describe negative enlargements of shapes	RH
Identify transformations of shapes	R
Perform and describe a series of transformations of shapes	
Identify invariant points and lines	H
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### Transforming and Constructing

Perform standard constructions using ruler and protractor or ruler and compasses	R
Solve loci problems	
Understand and use trigonometrical graphs	H
Sketch and identify translations of the graph of a given function	H
Sketch and identify reflections of the graph of a given function	H

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## Listing and Describing

Work with organised lists	
Sample spaces and probability	R
Use the product rule for counting	H
Complete and use Venn diagrams	R
Construct and interpret plans and elevations	R
Use data to compare distributions	R
Interpreting scatter diagrams	R

- denotes Higher Tier GCSE content
- R denotes 'review step' content should have been covered at KS3



#### Show that

- "Show that" with number
- "Show that" with algebra
- "Show that" with shape
- "Show that" with angles
- "Show that" with data
- "Show that" with vectors
- "Show that" with congruent triangles
- Formal proof with congruent triangles
  - H denotes Higher Tier GCSE content
  - R denotes 'review step' content should have been covered at KS3